

MOIRCS Deep Survey V: A Universal Relation for Stellar Mass and Surface Brightness of Galaxies

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ABSTRACT

We present a universal linear correlation between the stellar mass and surface brightness (SB) of galaxies at $0.3 < z < 3$, using a deep K -band selected catalog in the GOODS-North region. The correlation has a nearly constant slope, independent of redshift and color of galaxies in the rest- z frame. Considering unresolved compact galaxies, the tight correlation gives a lower boundary of SB for a given stellar mass; lower SB galaxies are prohibited over the boundary. The universal slope suggests that the stellar mass in galaxies was build up over their cosmic histories in a similar manner irrelevant to galaxy mass, as oppose to the scenario that massive galaxies mainly accumulated their stellar mass by major merging. In contrast, SB shows a strong dependence on redshift for a given stellar mass. It evolves as $\sim (1+z)^{-2.0 \sim -0.8}$, in addition to dimming as $(1+z)^4$ by the cosmological expansion effect. The brightening depends on galaxy color and stellar mass. The blue population (rest-frame $U - V < 0$), which is dominated by young and star-forming galaxies, evolves as $\sim (1+z)^{-0.8 \pm 0.3}$ in the rest- V band. On the other hand, the red population ($U - V > 0$) and the massive galaxies ($M_* > 10^{10} M_\odot$) shows stronger brightening, $(1+z)^{-1.5 \pm 0.1}$. Based on the comparison with galaxy evolution models, we find that the phenomena are well explained by the pure luminosity evolution of galaxies out to $z \sim 3$.

Subject headings: galaxies: evolutions — galaxies: fundamental parameters (surface brightness) — galaxies: high-redshift — infrared: galaxies

1. Introduction

Galaxy evolution from high- z to the present time is one of the central issues to be understood in Λ CDM paradigm. Among many parameters to characterize galaxies, stellar mass, which is accumulated in a galaxy with aging, is one of the most fundamental quantities for understanding the star-

forming and merging histories of galaxies. The surface brightness (SB) of galaxies is also key to studying galaxy structure. For example, Kormendy (1977) showed a tight correlation between SB and radius parameters for compact and normal galaxies. Since then, many authors have studied the evolution of SB in the high- z universe (e.g., Jorgensen et al. 1995; Roche et al. 1998; Lilly

et al. 1998; La Barbera et al. 2004; Barden et al. 2005; Ferreras et al. 2009; Trujillo 2004, 2006; Cimatti et al. 2008; van Dokkum et al. 2008; Muzzin et al. 2009; Damjanov et al. 2009). The SB and its correlation with other structural parameters of local galaxies were investigated with SDSS galaxies (e.g., Shen et al. 2003; Bernardi et al. 2003). A direct evidence of SB dimming as $(1+z)^4$ also intrigues us as a cosmological expansion test (Tolman 1930; Lubin & Sandage 2001).

By analogy with the Kormendy relation, the correlation of stellar mass with SB of galaxies (hereafter called the stellar-mass Kormendy relation) in the high- z universe will give us a clue to understanding the history of stellar mass built up in galaxies over cosmic time. In that context, we will study the correlation and its evolution from $z \sim 3$ to $z \sim 0.3$, using a deep K -selected galaxy catalog.

In §2, we describe the catalog we used. The data analysis and the result for the stellar-mass Kormendy relation and its evolution are detailed in §3 and §4. The results are discussed in §5. We use the AB magnitude system, except for Vega $U - V$ color.

2. Data

We use the K -band selected catalog of the MOIRCS Deep Survey (MODS) in the GOODS–North region (Kajisawa et al. 2009, hereafter K09), which is based on our imaging observations in JHK s bands with MOIRCS (Suzuki et al. 2008) and archived data. Four MOIRCS pointings cover 70% of the GOODS–North region (103 arcmin^2 , hereafter referred as ‘wide’ field). One of the four pointings, which includes HDF-N (Williams et al. 1996), is the ultra-deep field of MODS (28 arcmin^2 , ‘deep’ field). The deep imaging gives us SB data in a wide dynamic range, so that it is also advantageous for studying low SB galaxies at high redshift, where SB dimming due to the cosmological expansion is significant.

Although the detection completeness (90%) of the catalog is $K \sim 25 \text{ mag}$ for the wide field and $\sim 26 \text{ mag}$ for the deep field, we include fainter galaxies, because the K -band limit does not concern the present study. In fact, the sample with $K = 25$ limit gives the same result within error. Instead, we will take account of the size and SB

limits of galaxies. The FWHMs of the final stacked images are $0''.46$ for the deep image and $0''.53$ – $0''.60$ for the wide image. The numbers of galaxies are 3717 and 6265, respectively.

To obtain stellar-mass functions of MODS samples, K09 performed SED fitting of the multi-band photometry ($UBVizJHK$, $3.6 \mu\text{m}$, $4.5 \mu\text{m}$, and $5.8 \mu\text{m}$) with population synthesis models. We adopt the results with GALAXEV templates (Bruzual & Charlot 2003) and the Salpeter initial mass function (see K09 for more details). In the present analysis, the near-infrared data ($3.6 \mu\text{m}$) of Spitzer/IRAC are available for most of the sample galaxies (96%), so that SED fitting is reasonably reliable for the photometry at rest- z ($\lambda_{\text{eff}} = 0.9 \mu\text{m}$) or shorter wavelengths out to redshift ~ 3 .

3. Analyses

3.1. Stellar-mass Kormendy Relation

The surface brightness μ_K (mag arcsec^{-2}) in K band of the sample galaxies is defined as the brightness in two times the Kron radius, i.e.,

$$\mu_K = m_K + 2.5 \log(\pi R^2), \quad (1)$$

where m_K is total magnitude and R is two times the Kron radius r ($R = 2r$) in units of arcsec. For m_K , we use MAG_AUTO obtained by SExtractor (Bertin & Arnouts 1996), which gives the most precise estimate of the total magnitude of galaxies. Kron radius is defined as the first moment,

$$r = \frac{\sum r' I(r')}{\sum I(r')}, \quad (2)$$

where r' is isophotal radius and I is flux at r' . About 90% or more of the total light is within R , irrespective of galaxy shapes or redshifts (Kron 1980).

The half-light radius and central SB of galaxies have been investigated in many previous studies. However, in contrast, it is less reliable at higher redshifts in the present sample because of seeing effects. Therefore, we study the total SB in R instead. Figure 1 shows μ_K versus stellar mass (M_*) of all galaxies broken into redshift bins.

3.2. Point-like Sources

In order to examine the error of SB, we first study the reliability of the Kron radius of galaxies. Figure 2 shows the Kron radius derived by

SExtractor versus m_K for all MODS samples. We draw a boundary line above the stars, which are spectroscopically confirmed. Since spectroscopic data were not available for stars fainter than ~ 24 mag in the present region, we examined the Kron radius using artificial stars. The point sources were convolved with a gaussian point spread function (FWHM= $0''.5$), and then buried in the image with the same noise ($\sigma = 30.9$ mag pixel $^{-2}$) with that of the deep image. SExtractor was applied to the artifacts in the same manner as for the MODS catalog. The results are plotted over Figure 2. The objects below the boundary in Figure 2 are considered as point-like or unresolved sources in the following.

3.3. Monte Carlo Study with Mock Galaxies

Seeing and background noise strongly affect the observed Kron radius, especially for faint or small galaxies. To examine the effect, we generated mock galaxies with a 1/4-law or exponential profile and buried them in the simulated noise image. The galaxies were randomly generated with various magnitudes and effective or scale lengths, then analyzed with SExtractor in the same manner as for the MODS catalog. The result is shown in Figure 3. The observed Kron radii r are seriously affected by seeing for galaxies with an original Kron radius $r_0 \lesssim 0''.4$. The observed SB of the mock galaxies with $r_0 \lesssim 0''.4$ is systematically fainter than the originals. We note that faint SB galaxies are strongly affected by background noise. For example, the large scatter at $\log(r/r_0) < 0$ in Figure 3 is mainly due to low SB galaxies with $SB \gtrsim 26$ mag arcsec $^{-2}$. Figure 3 also shows that the SB of galaxies with observed $SB > 26$ mag arcsec $^{-2}$ is unreliable. Therefore, we will exclude the galaxies with $r \lesssim 0''.4$ and/or $SB > 26$ mag arcsec $^{-2}$ from the following discussion.

3.4. K – Corrections

Although a universal correlation independent on redshift is suggested in Figure 1, when we discuss the evolution of the correlation as a function of redshift, k -correction should be applied to the observed m_K to compare them at the same rest-frame wavelengths. The SB, $\mu_{\text{rest}}(\lambda)$ in a rest frame at wavelength λ , is obtained from the observed data and the model SED, using the equa-

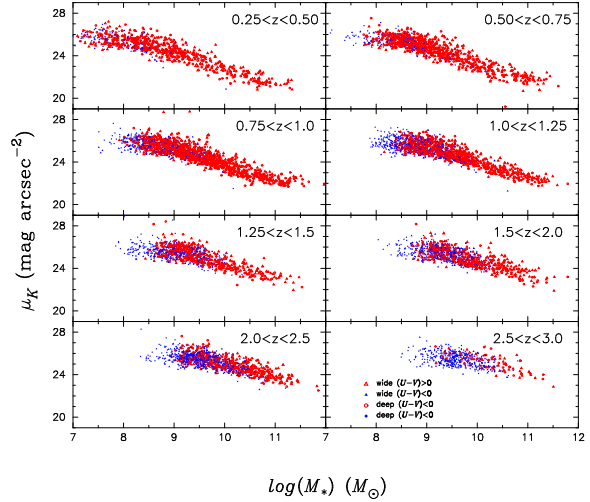


Fig. 1.— Correlation of surface brightness in K band (μ_K) with stellar mass (M_*) of galaxies for each redshift bin. The galaxies are classified according to the color (rest-frame $U - V$) and the regions (wide and deep) as shown in the bottom right frame.

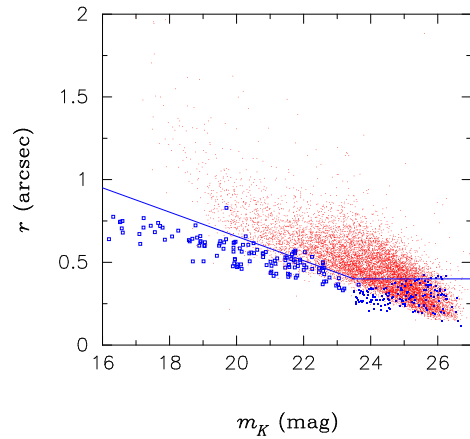


Fig. 2.— Kron radius r and total magnitude m_K for the MODS catalog. Squares show spectroscopically confirmed stars. The results of SExtractor for artificial stars are plotted by filled circles. The solid line delineates the upper boundary of point-like or unresolved sources.

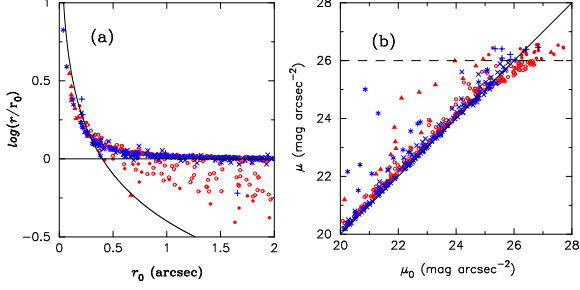


Fig. 3.— (a) Kron radius and (b) surface brightness for mock galaxies. The abscissa is the original values and the ordinate is those derived with SExtractor. Crosses (blue) and circles (red) show galaxies with 1/4-law and exponential profiles, respectively. The galaxies with $\mu > 26$ are depicted with filled circles and pluses. The solid curve in (a) is the observed Kron radius $r = 0.4$. The galaxies below the curve are noted with filled triangles and asterisks in (a) and (b). The galaxies below the solid curve at $r = 0.4$ in (a) and above the dashed line at $\mu = 26$ are excluded from the present study.

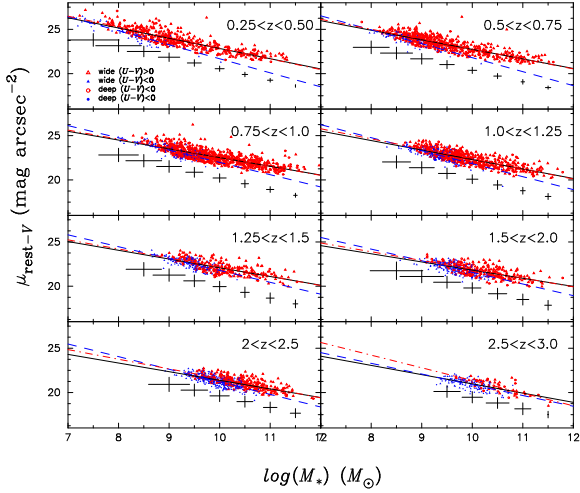


Fig. 4.— Same as Figure 1, but for the rest- V frame obtained with Equation 3. Typical errors are depicted by crosses for mass bins. Solid, dash, and dash-dot lines are the linear fits for all, blue ($U - V < 0$), and red ($U - V \geq 0$) samples, respectively.

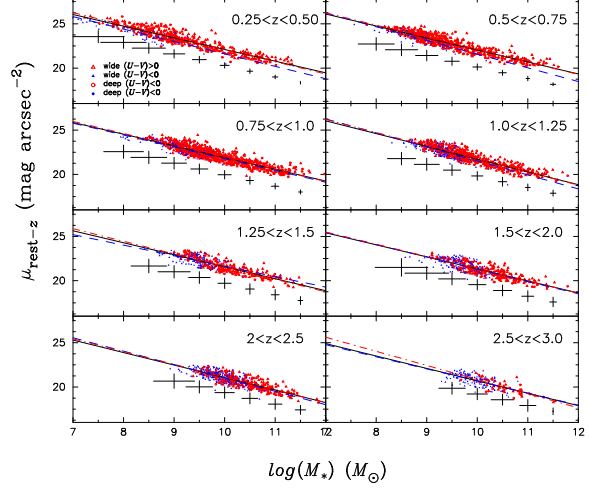


Fig. 5.— Same as Figure 4, but for the rest- z frame.

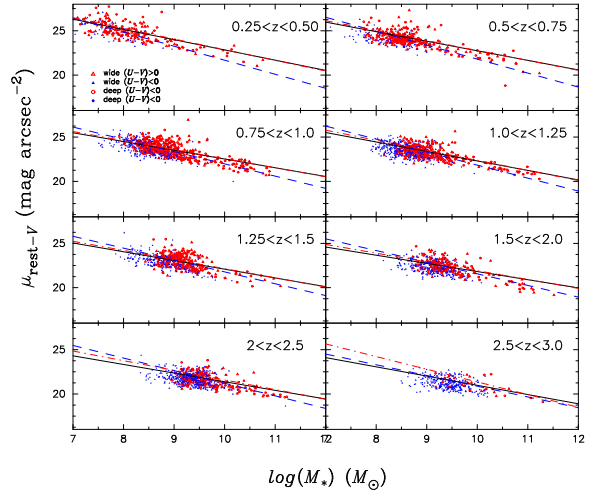


Fig. 6.— Same as Figure 4, but for discarded galaxies. The same regression lines as in Figure 4 are shown for reference.

tion,

$$\mu_{\text{rest}}(\lambda) = m_K + k(\lambda) + 2.5\log(\pi R^2) - 2.5\log(1+z)^3, \quad (3)$$

where $k(\lambda)$ is the k -correction defined as the color $k(\lambda) = (\text{rest-}V - K)$ or $(\text{rest-}z - K)$ of the best SED model fitted to the observations by the χ^2 analysis (K09).

We apply the k -correction to m_K for each sample galaxy to obtain the SB in the rest- V and z bands. The last term $(1+z)^3$ is the correction for the dimming effect due to the cosmological expansion, after m_K in AB system is reinstated by a factor of $(1+z)$. Figures 4 and 5 shows the correlation of M_* and SB in the rest- V and z frames, respectively. The point-like galaxies ($r < 0''.4$) and the galaxies with $\mu_K > 26$ mag arcsec $^{-2}$ are discarded from the analysis. The discarded objects are depicted separately in Figure 6 for comparison. Since the sizes of galaxies are suggestive of independence on wavelengths in the local universe (e.g., Shen et al. 2003; Bernardi et al. 2003) and at high redshift (e.g., Cassata et al 2009 at $z \sim 2$), no k -correction for galaxy size is applied in the present analysis.

3.5. Error Estimate

The errors in stellar mass and k -correction mainly originated from SED fitting and the photometric errors of the observations. In the course of χ^2 fitting to obtain a best SED model with various parameters (e.g., star-formation time scale, photometric redshift for galaxies with no spectroscopic redshift available, age, extinction, and metallicity), the probability distributions of stellar mass and k -correction can be calculated, where the photometry and photometric-redshift errors are included. The error for the observed SB is examined with mock galaxies in Figure 3 as a function of Kron radius. The photo- z error for galaxies with no spectroscopic redshift was studied in K09. From these errors, we obtained 1- σ errors for stellar mass and surface brightness for each galaxy in the rest- V and rest- z bands. The average errors for the stellar-mass bins are depicted in Figures 4 and 5.

4. Results

We obtain the least square fit of rest- V (rest- z) SB to M_* for the galaxies in Figure 4 (Figure 5)

with a linear regression,

$$\mu_{\text{rest}} = a(\log M_* - 10) + \mu_{\text{rest}}^{10}, \quad (4)$$

where μ_{rest}^{10} is SB at $M_* = 10^{10}M_\odot$ in the rest frame.

Since our image quality is not high enough for classifying the galaxies into morphological classes at high- z , we divided the samples into two groups according to rest-frame $U - V$ color and obtained again the linear fit for each group. Rest-frame $U - V = 0$ corresponds to the color of A0 stars, so that the bluer group is supposed to be dominated by young and star-forming galaxies. The results of the regression analysis with mean error are summarized in Table 1. The dispersion, σ , of the linear fit is listed in the last column. (For galaxies with $M_* > 10^{10}M_\odot$, the average SBs are obtained instead of linear fitting.) Figure 7 shows a , the slope of Equation 4, as a function of redshift for each group. The figure indicates no noticeable systematic redshift dependence, except a hint that the high redshift slope is slightly steeper than the values at lower redshift in rest- V for the blue group, though the error is large.

The offset μ_{rest}^{10} is plotted in Figure 8 as a function of redshift for each sample. Since the SBs depend on redshift for a given mass, we fit μ_{rest}^{10} in Figure 8 with redshift dependence,

$$\mu_{\text{rest}}^{10} = \mu_0 + 2.5\log(1+z)^n. \quad (5)$$

The results are shown in Figure 8 and Table 2.

The results, corrected for dust extinction, are also listed in Table 2, where the extinction is given from the best fit SED model by K09. It should be noted that the dust extinction in galaxies is a less reliable parameter in SED fitting (K09).

5. Discussion

We have obtained the linear correlation between the SB and stellar mass of galaxies in the GOODS-N region at $0.3 < z < 3$, which is an analogy of the Kormendy relation. The correlation has a nearly constant slope independent of redshift and the color of galaxies, especially in the rest- z frame. Although the low-mass limit of the observations depends on redshift, the similar slopes of the linear regression in different redshift bins are suggestive of a universal relation between the SB

TABLE 1
LINEAR FIT OF THE SURFACE BRIGHTNESS IN REST- V AND REST- z FRAMES TO STELLAR MASS OF GALAXIES.

Redshift	Sample	N	a	rest- V μ_{rest}^{10} (mag arcsec $^{-2}$)	σ	a	rest- z μ_{rest}^{10} (mag arcsec $^{-2}$)	σ
$0.25 \leq z < 0.50$	all	491	-1.16 ± 0.03	22.84 ± 0.04	0.58	-1.32 ± 0.02	22.10 ± 0.03	0.48
	$U - V < 0$	68	-1.58 ± 0.09	21.68 ± 0.16	0.46	-1.40 ± 0.08	21.60 ± 0.16	0.45
	$U - V \geq 0$	423	-1.21 ± 0.03	22.86 ± 0.04	0.55	-1.38 ± 0.03	22.11 ± 0.03	0.45
	$M_* > 10^{10} M_{\odot}^{\text{a}}$	92		22.23 ± 0.04	0.41		21.28 ± 0.05	0.44
$0.50 \leq z < 0.75$	all	626	-1.08 ± 0.03	22.74 ± 0.03	0.52	-1.35 ± 0.02	22.05 ± 0.02	0.43
	$U - V < 0$	83	-1.58 ± 0.09	21.80 ± 0.12	0.39	-1.55 ± 0.09	21.57 ± 0.12	0.38
	$U - V \geq 0$	543	-1.12 ± 0.03	22.77 ± 0.03	0.51	-1.39 ± 0.02	22.07 ± 0.02	0.42
	$M_* > 10^{10} M_{\odot}^{\text{a}}$	144		22.12 ± 0.05	0.61		21.22 ± 0.05	0.58
$0.75 \leq z < 1.0$	all	930	-0.99 ± 0.02	22.53 ± 0.02	0.51	-1.32 ± 0.02	21.90 ± 0.01	0.42
	$U - V < 0$	152	-1.38 ± 0.08	21.98 ± 0.09	0.43	-1.33 ± 0.08	21.78 ± 0.08	0.41
	$U - V \geq 0$	778	-1.02 ± 0.03	22.56 ± 0.02	0.52	-1.36 ± 0.02	21.91 ± 0.02	0.42
	$M_* > 10^{10} M_{\odot}^{\text{a}}$	302		21.96 ± 0.03	0.61	21.08 ± 0.04	0.62	
$1.0 \leq z < 1.25$	all	698	-1.07 ± 0.03	22.30 ± 0.02	0.49	-1.44 ± 0.03	21.72 ± 0.02	0.44
	$U - V < 0$	184	-1.47 ± 0.10	21.84 ± 0.07	0.45	-1.58 ± 0.10	21.52 ± 0.08	0.47
	$U - V \geq 0$	514	-1.13 ± 0.03	22.37 ± 0.02	0.48	-1.48 ± 0.03	21.76 ± 0.02	0.42
	$M_* > 10^{10} M_{\odot}^{\text{a}}$	201		21.67 ± 0.04	0.63		20.83 ± 0.04	0.63
$1.25 \leq z < 1.5$	all	396	-0.99 ± 0.04	22.08 ± 0.03	0.51	-1.35 ± 0.04	21.57 ± 0.02	0.44
	$U - V < 0$	151	-1.34 ± 0.11	21.78 ± 0.07	0.42	-1.18 ± 0.11	21.65 ± 0.07	0.44
	$U - V \geq 0$	245	-1.03 ± 0.06	22.14 ± 0.03	0.54	-1.43 ± 0.05	21.60 ± 0.03	0.44
	$M_* > 10^{10} M_{\odot}^{\text{a}}$	124		21.65 ± 0.06	0.62		20.90 ± 0.06	0.64
$1.5 \leq z < 2.0$	all	430	-0.92 ± 0.05	21.82 ± 0.02	0.51	-1.36 ± 0.04	21.33 ± 0.02	0.47
	$U - V < 0$	174	-1.31 ± 0.11	21.56 ± 0.05	0.45	-1.39 ± 0.12	21.30 ± 0.06	0.51
	$U - V \geq 0$	256	-0.99 ± 0.06	21.91 ± 0.04	0.52	-1.38 ± 0.06	21.35 ± 0.03	0.45
	$M_* > 10^{10} M_{\odot}^{\text{a}}$	177		21.40 ± 0.05	0.62		20.66 ± 0.05	0.64
$2.0 \leq z < 2.5$	all	565	-0.97 ± 0.04	21.38 ± 0.02	0.47	-1.41 ± 0.04	21.07 ± 0.02	0.44
	$U - V < 0$	294	-1.42 ± 0.07	21.21 ± 0.03	0.42	-1.51 ± 0.08	21.03 ± 0.03	0.45
	$U - V \geq 0$	271	-1.09 ± 0.06	21.58 ± 0.04	0.46	-1.44 ± 0.05	21.11 ± 0.04	0.44
	$M_* > 10^{10} M_{\odot}^{\text{a}}$	347		20.91 ± 0.03	0.61		20.39 ± 0.04	0.71
$2.5 \leq z < 3.0$	all	184	-1.04 ± 0.08	20.98 ± 0.04	0.48	-1.40 ± 0.09	20.70 ± 0.04	0.51
	$U - V < 0$	127	-1.21 ± 0.12	20.88 ± 0.04	0.44	-1.37 ± 0.15	20.68 ± 0.05	0.53
	$U - V \geq 0$	57	-1.43 ± 0.15	21.36 ± 0.10	0.48	-1.59 ± 0.15	20.84 ± 0.09	0.46
	$M_* > 10^{10} M_{\odot}^{\text{a}}$	104		20.57 ± 0.06	0.64		20.14 ± 0.07	0.72

^aAverage for galaxies with $M_* > 10^{10} M_{\odot}$

TABLE 2
REDSHIFT DEPENDENCE OF THE SURFACE BRIGHTNESS.

Sample	n	μ_0 (mag arcsec $^{-2}$)
rest- V		
all	-1.74 ± 0.13	23.63 ± 0.12
$U - V \geq 0$	-1.46 ± 0.07	23.49 ± 0.07
$U - V < 0$	-0.78 ± 0.25	22.28 ± 0.24
$M_* > 10^{10} M_\odot$	-1.53 ± 0.14	22.92 ± 0.13
rest- V (extinction corrected)		
all	-1.97 ± 0.10	23.13 ± 0.09
$U - V \geq 0$	-1.78 ± 0.10	23.04 ± 0.09
$U - V < 0$	-1.48 ± 0.26	22.47 ± 0.25
$M_* > 10^{10} M_\odot$	-1.85 ± 0.10	22.24 ± 0.10
rest- z		
all	-1.30 ± 0.11	22.71 ± 0.10
$U - V \geq 0$	-1.22 ± 0.09	22.68 ± 0.08
$U - V < 0$	-0.83 ± 0.22	22.13 ± 0.21
$M_* > 10^{10} M_\odot$	-1.05 ± 0.09	21.75 ± 0.09
rest- z (extinction corrected)		
all	-1.42 ± 0.10	22.44 ± 0.09
$U - V \geq 0$	-1.38 ± 0.09	22.43 ± 0.09
$U - V < 0$	-1.21 ± 0.24	22.24 ± 0.23
$M_* > 10^{10} M_\odot$	-1.22 ± 0.09	21.39 ± 0.09

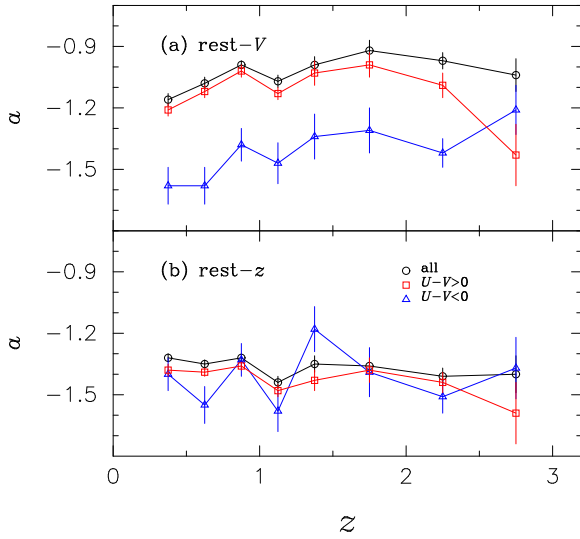


Fig. 7.— Slope a of the linear regression in Equation 4 as a function of redshift for each group in (a) rest- V and (b) rest- z frames.

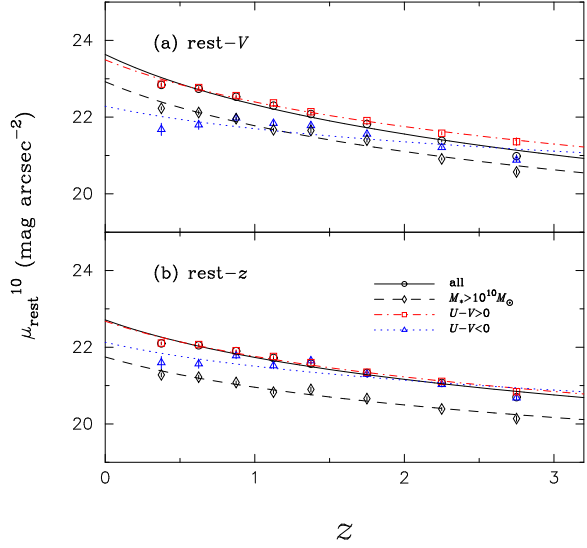


Fig. 8.— Surface brightness (μ_{rest}^{10}) at $M_* = 10^{10} M_\odot$ as a function of redshift. Diamonds are the average SB for $M_* > 10^{10} M_\odot$. Extinction is not corrected. The line is the fitting result for each group (Table 2).

and stellar mass of galaxies in a wide mass range. The stellar system of galaxies keeps the tight correlation over the cosmic time.

Considering that the light in the rest- z band is dominated by old stars and therefore traces the stellar mass, we note that the result should demonstrate a universal relation between surface stellar-mass density and stellar mass of galaxies. This finding indicates that stellar mass in galaxies was build up over cosmic time in a similar manner, irrelevant to galaxy mass, as opposed to the scenario that massive galaxies mainly accumulated their stellar mass by major merging. Dissipationless merging increases the size of galaxies, which leads to lower SB (Navarro 1990; Boylan-Kolchin, Ma, & Quataert 2006; McIntosh et al. 2005; Damjanov et al. 2009; Nipoti et al. 2009). If dry merging is a more important process for more massive galaxies, as conjectured from Λ CDM model, then the slope should become shallower at lower redshifts for massive galaxies.

Figure 8 shows the redshift dependence of μ_{rest}^{10} . As a whole, SB is brighter at higher redshifts for a given mass. The brightening obeys the relation with $n = -2.0 \sim -0.8$ in rest- V and $n = -1.4 \sim -0.8$ in rest- z , depending on the subgroups and extinction correction used. In Figure 9, we compare the observed SB of galaxies with the luminosity evolution, for a given stellar mass with no size change, for two extreme cases, i.e. a constant star formation (SF) model and an instantaneous-burst galaxy model formed at $z_f = 9$ (Bruzual & Charlot 2003). It is noted that we discuss the properties of galaxies with same stellar mass at any redshifts, not tracing the evolution of mass or luminosity for a certain galaxy. The SB evolution of red ($U - V > 0$) and blue ($U - V < 0$) samples is well reproduced by the luminosity evolution models of burst and constant SF models, respectively, though SB is a little bluer than the models at higher redshift. However, the models depend on various parameters (e.g., z_f , metallicity, star-formation rate, extinction, etc). For example, lower metallicity at higher redshift makes the color bluer, which gives an evolution more consistent with the observation. In any case, our result supports the scenario that galaxies accumulate stellar mass mainly by star formation.

The different selection criteria and analysis would not facilitate the direct comparison of the

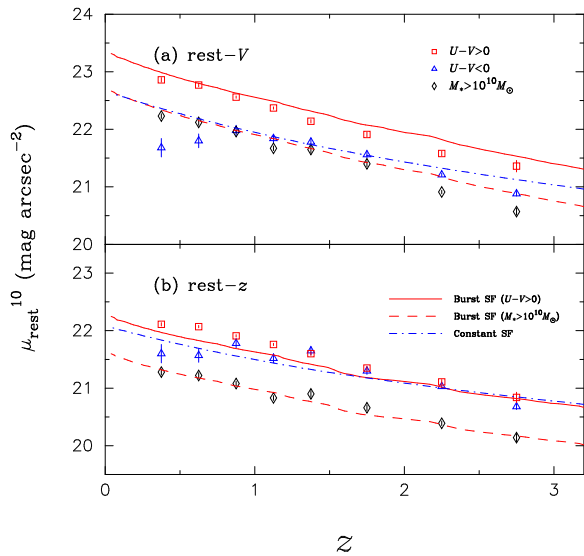


Fig. 9.— Comparison of the observed surface brightness for blue, red, and massive samples with the luminosity evolution, for a given stellar mass, with a constant star-formation model (dash-dot line) and an instantaneous-burst galaxy model (solid and dash lines) formed at $z_f = 9$ (Bruzual & Charlot 2003). The models are arbitrarily offset at the rest- V band to fit the observations.

present result with those of previous studies, which discussed luminosity evolution mainly in half-light radius based on images with a high spatial resolution. The studies at high redshifts could be biased toward compact and massive galaxies. In contrast, we focus on more general galaxies and studied the evolution of their SB based on the Kron radius for a given mass, making use of our deep imaging data, which are favorable for diffuse galaxies. Despite of the difference, the present results are consistent with previous studies.

For example, our result for the blue population supports the finding of Barden et al. (2005) that the average surface brightness of disk galaxies increases with redshift by about 1 mag to $z \sim 1$ for galaxies. Ferguson et al. (2004) and Akiyama et al. (2008) showed the size evolution of LBG galaxies at high redshifts, which indicates much stronger SB brightening than our results. Although the blue group includes most LBGs in our catalog (Ichikawa et al. 2007), our different selection criteria sample various populations of more general star-forming galaxies with low stellar mass, which would have more moderate evolution (Trujillo et al. 2004; Trujillo et al. 2006). The results for red massive groups are also in good agreement with those in previous studies. Early-type galaxies were brighter by $1 \sim 2$ mag at $z \sim 1$ (McIntosh et al. 2005) and $z \sim 1.5$ (Damjanov et al. 2009), which would correspond to our red group.

Trujillo et al. (2007) for galaxies with $M_* > 10^{11} M_\odot$ and Toft et al. (2009) for those with $M_* > 5 \times 10^{10} M_\odot$ showed that massive galaxies were much smaller in the past than their local massive counterparts and the evolution was particularly strong for the highly concentrated objects, which are supposed to be high SB galaxies. Since our sample includes few such massive galaxies, we calculated the average SB and its evolution in galaxies with $M_* > 10^{10} M_\odot$ for comparison. The result is in good agreement with their results for resolved galaxies. Their finding that the evolution is stronger for spheroid-like or quiescent galaxies would be supported by our result for the galaxies with the dust extinction corrected (Table 2).

Finally we emphasize that the present study has not only confirmed the previous studies on the SB evolution of galaxies, but also demonstrated

that the brightening dates back to $z \sim 3$. We should also mention about the point-like or unresolved galaxies ($r < 0''.4$), which are excluded from the analysis for the present stellar-mass Kormendy relation. For example, early-type galaxies (Damjanov et al. 2009) and compact galaxies (van Dokkum et al. 2008) tended to be a factor 2–5 smaller in half light radius than local counterparts of similar mass. The SBs of galaxies at the faint-end limit of each redshift bin in Figure 6 are seriously affected by background noise, while more massive galaxies would not. The real SB of the massive galaxies, which are well above the SB limit but unresolved in the present observation, could be much brighter. The samples of e.g., Akiyama et al. (2008), Trujillo et al. (2007), and Muzzin et al. (2009) would be such galaxies as those we did not resolve with our poorer image size. If they are observed with higher spatial resolution, they could be plotted further below the regression lines in Figures 4 and 5. Therefore, the stellar-mass Kormendy relation presented in this paper would rather show a lower boundary of the correlation of stellar mass and SB of galaxies; lower SB galaxies are prohibited over the boundary.

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